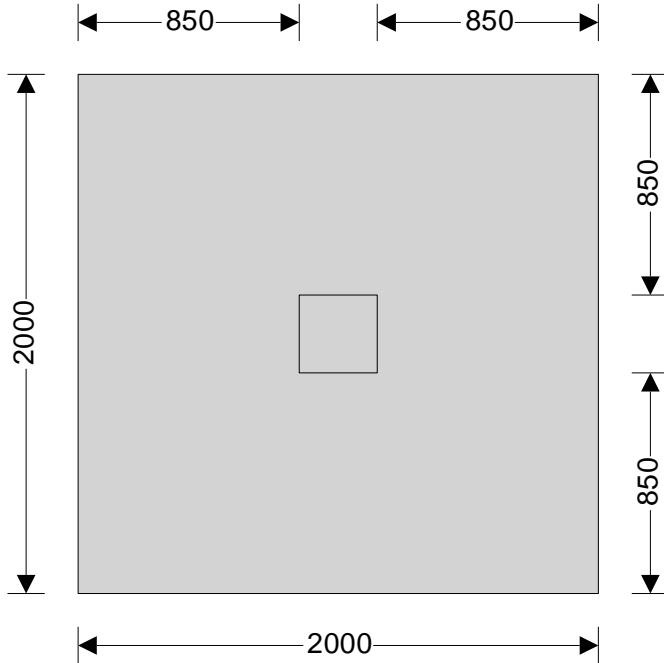


PAD FOOTING ANALYSIS AND DESIGN (BS8110-1:1997)

Tedds calculation version 2.0.07


Pad footing details

Length of pad footing	L = 2000 mm
Width of pad footing	B = 2000 mm
Area of pad footing	A = L × B = 4.000 m²
Depth of pad footing	h = 600 mm
Depth of soil over pad footing	h_{soil} = 750 mm
Density of concrete	ρ_{conc} = 24.0 kN/m³

Column details

Column base length	l_A = 300 mm
Column base width	b_A = 300 mm
Column eccentricity in x	e_{PxA} = 0 mm
Column eccentricity in y	e_{PyA} = 0 mm

Soil details

Cohesive soil

Density of soil	ρ_{soil} = 18.0 kN/m³
Design shear strength	ϕ' = 25.0 deg
Design base friction	δ = 19.3 deg
Allowable bearing pressure	P_{bearing} = 250 kN/m²

Axial loading on column

Dead axial load on column	P_{GA} = 500.0 kN
Imposed axial load on column	P_{QA} = 300.0 kN

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Wind axial load on column

$$P_{WA} = \mathbf{0.0 \text{ kN}}$$

Total axial load on column

$$P_A = \mathbf{800.0 \text{ kN}}$$

Foundation loads

Dead surcharge load

$$F_{Gsur} = \mathbf{0.000 \text{ kN/m}^2}$$

Imposed surcharge load

$$F_{Qsur} = \mathbf{0.000 \text{ kN/m}^2}$$

Pad footing self weight

$$F_{swt} = h \times \rho_{conc} = \mathbf{14.400 \text{ kN/m}^2}$$

Soil self weight

$$F_{soil} = h_{soil} \times \rho_{soil} = \mathbf{13.500 \text{ kN/m}^2}$$

Total foundation load

$$F = A \times (F_{Gsur} + F_{Qsur} + F_{swt} + F_{soil}) = \mathbf{111.6 \text{ kN}}$$

Calculate pad base reaction

Total base reaction

$$T = F + P_A = \mathbf{911.6 \text{ kN}}$$

Eccentricity of base reaction in x

$$e_{Tx} = (P_A \times e_{PxA} + M_{xA} + H_{xA} \times h) / T = \mathbf{0 \text{ mm}}$$

Eccentricity of base reaction in y

$$e_{Ty} = (P_A \times e_{PyA} + M_{yA} + H_{yA} \times h) / T = \mathbf{0 \text{ mm}}$$

Check pad base reaction eccentricity

$$\text{abs}(e_{Tx}) / L + \text{abs}(e_{Ty}) / B = \mathbf{0.000}$$

Base reaction acts within middle third of base

Calculate pad base pressures

$$q_1 = T / A - 6 \times T \times e_{Tx} / (L \times A) - 6 \times T \times e_{Ty} / (B \times A) = \mathbf{227.900 \text{ kN/m}^2}$$

$$q_2 = T / A - 6 \times T \times e_{Tx} / (L \times A) + 6 \times T \times e_{Ty} / (B \times A) = \mathbf{227.900 \text{ kN/m}^2}$$

$$q_3 = T / A + 6 \times T \times e_{Tx} / (L \times A) - 6 \times T \times e_{Ty} / (B \times A) = \mathbf{227.900 \text{ kN/m}^2}$$

$$q_4 = T / A + 6 \times T \times e_{Tx} / (L \times A) + 6 \times T \times e_{Ty} / (B \times A) = \mathbf{227.900 \text{ kN/m}^2}$$

$$q_{\min} = \min(q_1, q_2, q_3, q_4) = \mathbf{227.900 \text{ kN/m}^2}$$

$$q_{\max} = \max(q_1, q_2, q_3, q_4) = \mathbf{227.900 \text{ kN/m}^2}$$

PASS - Maximum base pressure is less than allowable bearing pressure

227.9 kN/m²

227.9 kN/m²

227.9 kN/m²

227.9 kN/m²

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Partial safety factors for loads

Partial safety factor for dead loads $\gamma_{fG} = 1.40$

Partial safety factor for imposed loads $\gamma_{fQ} = 1.60$

Partial safety factor for wind loads $\gamma_{fW} = 0.00$

Ultimate axial loading on column

Ultimate axial load on column $P_{uA} = P_{GA} \times \gamma_{fG} + P_{QA} \times \gamma_{fQ} + P_{WA} \times \gamma_{fW} = 1180.0 \text{ kN}$

Ultimate foundation loads

Ultimate foundation load $F_u = A \times [(F_{Gsur} + F_{swt} + F_{soil}) \times \gamma_{fG} + F_{Qsur} \times \gamma_{fQ}] = 156.2 \text{ kN}$

Ultimate horizontal loading on column

Ultimate horizontal load in x direction $H_{xuA} = H_{GxA} \times \gamma_{fG} + H_{QxA} \times \gamma_{fQ} + H_{WxA} \times \gamma_{fW} = 0.0 \text{ kN}$

Ultimate horizontal load in y direction $H_{yuA} = H_{GyA} \times \gamma_{fG} + H_{QyA} \times \gamma_{fQ} + H_{WyA} \times \gamma_{fW} = 0.0 \text{ kN}$

Ultimate moment on column

Ultimate moment on column in x direction $M_{xuA} = M_{GxA} \times \gamma_{fG} + M_{QxA} \times \gamma_{fQ} + M_{WxA} \times \gamma_{fW} = 0.000 \text{ kNm}$

$M_{yuA} = M_{GyA} \times \gamma_{fG} + M_{QyA} \times \gamma_{fQ} + M_{WyA} \times \gamma_{fW} = 0.000 \text{ kNm}$

Calculate ultimate pad base reaction

Ultimate base reaction $T_u = F_u + P_{uA} = 1336.2 \text{ kN}$

$e_{Txu} = (P_{uA} \times e_{Pxu} + M_{xuA} \times h) / T_u = 0 \text{ mm}$

$e_{Tyu} = (P_{uA} \times e_{Pyu} + M_{yuA} \times h) / T_u = 0 \text{ mm}$

Calculate ultimate pad base pressures

$q_{1u} = T_u / A - 6 \times T_u \times e_{Txu} / (L \times A) - 6 \times T_u \times e_{Tyu} / (B \times A) = 334.060 \text{ kN/m}^2$

$q_{2u} = T_u / A - 6 \times T_u \times e_{Txu} / (L \times A) + 6 \times T_u \times e_{Tyu} / (B \times A) = 334.060 \text{ kN/m}^2$

$q_{3u} = T_u / A + 6 \times T_u \times e_{Txu} / (L \times A) - 6 \times T_u \times e_{Tyu} / (B \times A) = 334.060 \text{ kN/m}^2$

$q_{4u} = T_u / A + 6 \times T_u \times e_{Txu} / (L \times A) + 6 \times T_u \times e_{Tyu} / (B \times A) = 334.060 \text{ kN/m}^2$

$q_{minu} = \min(q_{1u}, q_{2u}, q_{3u}, q_{4u}) = 334.060 \text{ kN/m}^2$

$q_{maxu} = \max(q_{1u}, q_{2u}, q_{3u}, q_{4u}) = 334.060 \text{ kN/m}^2$

Minimum ultimate base pressure

Maximum ultimate base pressure

Calculate rate of change of base pressure in x direction

Left hand base reaction $f_{uL} = (q_{1u} + q_{2u}) \times B / 2 = 668.120 \text{ kN/m}$

Right hand base reaction $f_{uR} = (q_{3u} + q_{4u}) \times B / 2 = 668.120 \text{ kN/m}$

$L_x = L = 2000 \text{ mm}$

$C_x = (f_{uR} - f_{uL}) / L_x = 0.000 \text{ kN/m/m}$

Calculate pad lengths in x direction

Left hand length $L_L = L / 2 + e_{Pxu} = 1000 \text{ mm}$

Right hand length $L_R = L / 2 - e_{Pxu} = 1000 \text{ mm}$

Calculate ultimate moments in x direction

Ultimate moment in x direction $M_x = f_{uL} \times L_L^2 / 2 + C_x \times L_L^3 / 6 - F_u \times L_L^2 / (2 \times L) = 295.000 \text{ kNm}$

Calculate rate of change of base pressure in y direction

Top edge base reaction $f_{uT} = (q_{2u} + q_{4u}) \times L / 2 = 668.120 \text{ kN/m}$

Bottom edge base reaction $f_{uB} = (q_{1u} + q_{3u}) \times L / 2 = 668.120 \text{ kN/m}$

$L_y = B = 2000 \text{ mm}$

$C_y = (f_{uB} - f_{uT}) / L_y = 0.000 \text{ kN/m/m}$

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Calculate pad lengths in y direction

Top length

$$L_T = B / 2 - e_{PyA} = 1000 \text{ mm}$$

Bottom length

$$L_B = B / 2 + e_{PyA} = 1000 \text{ mm}$$

Calculate ultimate moments in y direction

Ultimate moment in y direction

$$M_y = f_{uT} \times L_T^2 / 2 + C_y \times L_T^3 / 6 - F_u \times L_T^2 / (2 \times B) = 295.000 \text{ kNm}$$

Material details

Characteristic strength of concrete

$$f_{cu} = 30 \text{ N/mm}^2$$

Characteristic strength of reinforcement

$$f_y = 500 \text{ N/mm}^2$$

Characteristic strength of shear reinforcement

$$f_{yv} = 250 \text{ N/mm}^2$$

Nominal cover to reinforcement

$$c_{nom} = 50 \text{ mm}$$

Moment design in x direction

Diameter of tension reinforcement

$$\phi_{xB} = 16 \text{ mm}$$

Depth of tension reinforcement

$$d_x = h - c_{nom} - \phi_{xB} / 2 = 542 \text{ mm}$$

Design formula for rectangular beams (cl 3.4.4.4)

$$K_x = M_x / (B \times d_x^2 \times f_{cu}) = 0.017$$

$$K_x' = 0.156$$

K_x < K_x' compression reinforcement is not required

Lever arm

$$z_x = d_x \times \min([0.5 + \sqrt{(0.25 - K_x / 0.9)}], 0.95) = 515 \text{ mm}$$

Area of tension reinforcement required

$$A_{s_x_req} = M_x / (0.87 \times f_y \times z_x) = 1317 \text{ mm}^2$$

Minimum area of tension reinforcement

$$A_{s_x_min} = 0.0013 \times B \times h = 1560 \text{ mm}^2$$

Tension reinforcement provided

12 No. 16 dia. bars bottom (175 centres)

Area of tension reinforcement provided

$$A_{s_x_B_prov} = N_{xB} \times \pi \times \phi_{xB}^2 / 4 = 2413 \text{ mm}^2$$

PASS - Tension reinforcement provided exceeds tension reinforcement required

Moment design in y direction

Diameter of tension reinforcement

$$\phi_{yB} = 16 \text{ mm}$$

Depth of tension reinforcement

$$d_y = h - c_{nom} - \phi_{xB} - \phi_{yB} / 2 = 526 \text{ mm}$$

Design formula for rectangular beams (cl 3.4.4.4)

$$K_y = M_y / (L \times d_y^2 \times f_{cu}) = 0.018$$

$$K_y' = 0.156$$

K_y < K_y' compression reinforcement is not required

Lever arm

$$z_y = d_y \times \min([0.5 + \sqrt{(0.25 - K_y / 0.9)}], 0.95) = 500 \text{ mm}$$

Area of tension reinforcement required

$$A_{s_y_req} = M_y / (0.87 \times f_y \times z_y) = 1357 \text{ mm}^2$$

Minimum area of tension reinforcement

$$A_{s_y_min} = 0.0013 \times L \times h = 1560 \text{ mm}^2$$

Tension reinforcement provided

10 No. 16 dia. bars bottom (200 centres)

Area of tension reinforcement provided

$$A_{s_y_B_prov} = N_{yB} \times \pi \times \phi_{yB}^2 / 4 = 2011 \text{ mm}^2$$

PASS - Tension reinforcement provided exceeds tension reinforcement required

Calculate ultimate shear force at d from top face of column

Ultimate pressure for shear

$$q_{su} = (q_{1u} - C_y \times (B / 2 + e_{PyA} + b_A / 2 + d_y) / L + q_{4u}) / 2$$

$$q_{su} = 334.060 \text{ kN/m}^2$$

Area loaded for shear

$$A_s = L \times (B / 2 - e_{PyA} - b_A / 2 - d_y) = 0.648 \text{ m}^2$$

Ultimate shear force

$$V_{su} = A_s \times (q_{su} - F_u / A) = 191.160 \text{ kN}$$

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Shear stresses at d from top face of column (cl 3.5.5.2)

Design shear stress

$$v_{su} = V_{su} / (L \times d_y) = 0.182 \text{ N/mm}^2$$

From BS 8110:Part 1:1997 - Table 3.8

Design concrete shear stress

$$v_c = 0.79 \text{ N/mm}^2 \times \min(3, [100 \times A_{s,yB_prov} / (L \times d_y)]^{1/3}) \times \max((400 \text{ mm} / d_y)^{1/4}, 0.67) \times (\min(f_{cu} / 1 \text{ N/mm}^2, 40) / 25)^{1/3} / 1.25 = 0.361 \text{ N/mm}^2$$

Allowable design shear stress

$$v_{max} = \min(0.8 \text{ N/mm}^2 \times \sqrt{(f_{cu} / 1 \text{ N/mm}^2)}, 5 \text{ N/mm}^2) = 4.382 \text{ N/mm}^2$$

PASS - $v_{su} < v_c$ - No shear reinforcement required

Calculate ultimate punching shear force at face of column

Ultimate pressure for punching shear

$$q_{puA} = q_{1u} + [(L/2 + e_{pxA} - l_A/2) + (l_A/2)] \times C_x / B - [(B/2 + e_{pyA} - b_A/2) + (b_A/2)] \times C_y / L = 334.060 \text{ kN/m}^2$$

Average effective depth of reinforcement

$$d = (d_x + d_y) / 2 = 534 \text{ mm}$$

Area loaded for punching shear at column

$$A_{pA} = (l_A) \times (b_A) = 0.090 \text{ m}^2$$

Length of punching shear perimeter

$$u_{pA} = 2 \times (l_A) + 2 \times (b_A) = 1200 \text{ mm}$$

Ultimate shear force at shear perimeter

$$V_{puA} = P_{uA} + (F_u / A - q_{puA}) \times A_{pA} = 1153.450 \text{ kN}$$

Effective shear force at shear perimeter

$$V_{puAeff} = V_{puA} = 1153.450 \text{ kN}$$

Punching shear stresses at face of column (cl 3.7.7.2)

Design shear stress

$$v_{puA} = V_{puAeff} / (u_{pA} \times d) = 1.800 \text{ N/mm}^2$$

Allowable design shear stress

$$v_{max} = \min(0.8 \text{ N/mm}^2 \times \sqrt{(f_{cu} / 1 \text{ N/mm}^2)}, 5 \text{ N/mm}^2) = 4.382 \text{ N/mm}^2$$

PASS - Design shear stress is less than allowable design shear stress

Calculate ultimate punching shear force at perimeter of 1.5 d from face of column

Ultimate pressure for punching shear

$$q_{puA1.5d} = q_{1u} + [L/2] \times C_x / B - [(B/2 + e_{pyA} - b_A/2 - 1.5 \times d) + (b_A + 2 \times 1.5 \times d)/2] \times C_y / L = 334.060 \text{ kN/m}^2$$

Average effective depth of reinforcement

$$d = (d_x + d_y) / 2 = 534 \text{ mm}$$

Area loaded for punching shear at column

$$A_{pA1.5d} = L \times (b_A + 2 \times 1.5 \times d) = 3.804 \text{ m}^2$$

Length of punching shear perimeter

$$u_{pA1.5d} = 2 \times L = 4000 \text{ mm}$$

Ultimate shear force at shear perimeter

$$V_{puA1.5d} = P_{uA} + (F_u / A - q_{puA1.5d}) \times A_{pA1.5d} = 57.820 \text{ kN}$$

Effective shear force at shear perimeter

$$V_{puA1.5deff} = V_{puA1.5d} \times 1.25 = 72.275 \text{ kN}$$

Punching shear stresses at perimeter of 1.5 d from face of column (cl 3.7.7.2)

Design shear stress

$$v_{puA1.5d} = V_{puA1.5deff} / (u_{pA1.5d} \times d) = 0.034 \text{ N/mm}^2$$

From BS 8110:Part 1:1997 - Table 3.8

Design concrete shear stress

$$v_c = 0.79 \text{ N/mm}^2 \times \min(3, [100 \times (A_{s,xB_prov} / (B \times d_x) + A_{s,yB_prov} / (L \times d_y))]^{1/3}) \times \max((800 \text{ mm} / (d_x + d_y))^{1/4}, 0.67) \times (\min(f_{cu} / 1 \text{ N/mm}^2, 40) / 25)^{1/3} / 1.25 = 0.370 \text{ N/mm}^2$$

Allowable design shear stress

$$v_{max} = \min(0.8 \text{ N/mm}^2 \times \sqrt{(f_{cu} / 1 \text{ N/mm}^2)}, 5 \text{ N/mm}^2) = 4.382 \text{ N/mm}^2$$

PASS - $v_{puA1.5d} < v_c$ - No shear reinforcement required

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